

GeMSS: A Great Multivariate Short Signature

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1 Introduction

*sparkling GeMSS spring up from the night sky
a dazzling splendor to ever beautify
sequined glories that verily eye smack
sparkling GeMSS spring up from night sky
studding the vast backdrop of black*

The purpose of this document is to present GeMSS : a Great Multivariate Signature Scheme. As suggested by its name, GeMSS is a multivariate-based [14, 22, 4, 2, 20, 19] signature scheme producing small signatures. It has a fast verification process, and a medium/large public-key. GeMSS is in direct lineage from QUARTZ [18] and borrows some design rationale of the Gui multivariate signature scheme [5]. The former schemes are built from the *Hidden Field Equations* cryptosystem (HFE) [17, published in 1996] by using the so-called minus and vinegar modifiers, i.e. HFEv- [12]. It is fair to say that HFE, and its variants, are the most studied schemes in multivariate cryptography. QUARTZ produces signatures of 128 bits for a security level of 80 bits and was submitted to the *Nessie Ecrypt* competition [15] for public-key signatures. In contrast to many multivariate schemes, no practical attack has been reported against QUARTZ. This is remarkable knowing the intense activity in the cryptanalysis of multivariate schemes, e.g. [16, 13, 7, 8, 11, 10, 6, 9, 4, 2, 3, 1, 19, 21]. The best known attack remains [8] that serves as a reference to set the parameters for GeMSS.

GeMSS is a faster variant of QUARTZ that incorporates the latest results in multivariate cryptography to reach higher security levels than QUARTZ whilst improving efficiency.

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2 Advantages and limitations (2.B.6)

Since the first scheme of Mastumoto and Imai [14] in 1988, almost 30 years ago, multivariate-based cryptosystems have been extensively analysed in the literature. We have designed GeMSS using this knowledge and taking conservative choices for deriving parameters. We also performed practical experiments using the best known tools for computing Gröbner bases.

From a practical point of view, the main drawback of GeMSS is the size of the public-key. However, we mention that the generation of a (public-key,secret-key) remains rather efficient in GeMSS. The main advantages of GeMSS are the size of the signatures generated, about 2λ bits, and the fast verification process.

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Aside from signature size and verification time, other performance characteristics of GeMSS raise some concerns. The signing time is quite high and the public keys are quite large; these properties may be features of GeMSS that are inherent to the HFEv-methodology. Decrease D and adapt the others parameters. No new attack Better understanding of the security Improved efficiency. Software New parameters short signature (258 bits), fast verification ($\approx 1\ \mu$ seconds), and large public-key (≈ 352 KBytes). RISQ. 15 / 15. GEMSS: The objective is to create a re-enforced surface in the runway strip, which is predominantly natural grass alongside the paved shoulder of runways. GEMSS is a new composite technology combining known materials, which have not been used together previously. The objective is to create a re-enforced surface in the runway strip, which is predominantly natural grass alongside the paved shoulder of runways. It supports aircraft after an excursion and substantially reduces the risk of damage to the aircraft.

@inproceedings{Casanova2017GeMSSAG, title={GeMSS: A Great Multivariate Short Signature}, author={Antoine Casanova and J. Faugère and Gilles Macario-Rat and Jacques Patarin and Ludovic Perret and Jocelyn Ryckeghem}, year={2017} }. The purpose of this document is to present GeMSS : a Great Multivariate Signature Scheme. As suggested by its name, GeMSS is a multivariate-based [14, 22, 4, 2, 20, 19] signature scheme producing small signatures. It has a fast verification process, and a medium/large public-key. GeMSS is in direct lineage from QUARTZ [18] and borrows some design rationale of the Gui multivariate signature scheme [5]. The former schemes are built from the Hidden Field Equations cryptosystem (HFE) [17, published]. Expand. Gemss: A great multivariate short signature. Jan 2017. A Casanova. Post-quantum cryptosystems have attracted a great interest, from researchers, latest. This work introduces two new forms of the hidden discrete logarithm problem and three new post-quantum signature schemes. The finite non-commutative associative algebras of two types are used as the algebraic support of the proposed cryptoschemes: i) containing a global two-sided unit and ii) containing a large ... GeMSS: A Great Multivariate Short Signature. PhD thesis, PhD thesis, UPMC-Paris 6 Sorbonne Universités, 2017. [8] M.-S. Chen, A. Hülsing, J. Rijneveld, S. Samardjiska, and P. Schwabe. MQDSS specifications. <http://mqdss.org/specification.html> . [9] E. Crockett, C. Paquin, and D. Stebila. Prototyping post-quantum and hybrid key exchange and authentication in tls and ssh. Cryptology ePrint Archive, Report 2019/858, 2019. <https://eprint.iacr.org/2019/858>.